

End of the list

More List Idioms

Friday, November 3, 2006



CS111 Computer Programming

Department of Computer Science
Wellesley College

Review: IntList Summation

```
public class IntListOps {  
    public static int sumList (IntList list) {  
        if (IntList.isEmpty(list)) { // base case  
            return 0;  
        } else { // recursive case  
            return IntList.head(list) + sumList(IntList.tail(list));  
        }  
    }  
}
```

Testing sumList in DrJava:

```
>IntListOps.sumList(IntList.fromString("[5,7,4]"))  
16
```

More lists 15a-2

Abbreviating IntList: Approach 1

```
public class IntListOps {  
    public static int sumList (IntList list) {  
        if (isEmpty(list)) {  
            return 0; // base case  
        } else { // recursive case  
            return head(list) + sumList(tail(list));  
        }  
    }  
    // Define local versions of IntList methods  
    public static int head (IntList L) {return IntList.head(L);}  
    // Similarly for isEmpty, tail, empty, prepend, fromList, ...  
}
```

Testing sumList in DrJava:

```
>IntListOps.sumList(IntList.fromString("[5,7,4]"))  
16
```

More lists 15a-3

Abbreviating IntList: Approach 2

```
public class IntListOps {  
    public static IntList IL;  
    public static int sumList (IntList list) {  
        if (IL.isEmpty(list)) {  
            return 0; // base case  
        } else { // recursive case  
            return IL.head(list) + sumList(IL.tail(list));  
        }  
    }  
}
```

Testing sumList in DrJava:

```
>IntList IL;  
>IntListOps ILO;  
>ILO.sumList(IL.fromString("[5,7,4]"))  
16
```

More lists 15a-4

Testing via the main method

```
public class IntListOps {  
    public static int sumList (IntList list) {...}  
  
    public static void main (String[] args) {  
        if (args.length == 2) {  
            IntList L = IntList.fromString(args[1]);  
            if (args[0].equals("sumList"))  
                System.out.println("sumList(" + L + ") = " + sumList(L));  
            else if ...  
        } else ...  
    }  
}
```

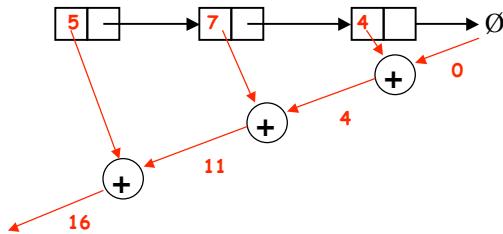
Testing sumList in DrJava:

```
>java IntListOps sumList [5,7,4]  
16
```

More lists 15a-5

sumList Illustrates the List Accumulation Idiom

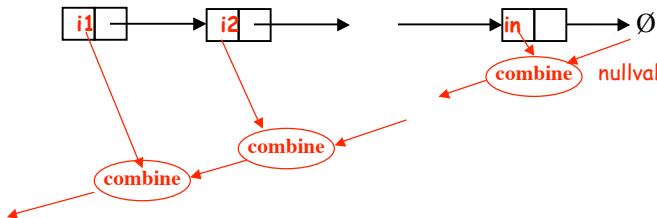
```
// Returns the sum of the elements of an integer list  
public static int sumList (IntList list) {  
    if (isEmpty(list)) {  
        return 0; // base case  
    } else {  
        head(list) + sumList(tail(list)) // recursive case  
    }  
}
```



More lists 15a-6

The General List Accumulation Idiom

```
// Need to instantiate the red parts
public static int accum (IntList list) {
    if (isEmpty(list)) {
        return nullval; // base case
    } else {
        combine(head(list),accum(tail(list))) // recursive case
    }
}
```



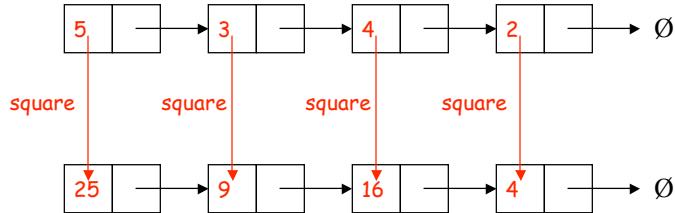
More lists 15a-7

Instantiating the List Accumulation Idiom

accum	combine(elt,ans)	nullval
sumList	elt + ans	0
prodList	elt * ans	1
length	1 + ans	0
minList	Math.min(elt,ans)	Integer.MAX_VALUE
maxList	Math.max(elt,ans)	Integer.MIN_VALUE
areAllPositive	(elt > 0) && ans	true
isSomePositive	(elt > 0) ans	false
copyList	prepend(elt,ans)	empty()
append	see later	see later

More lists 15a-8

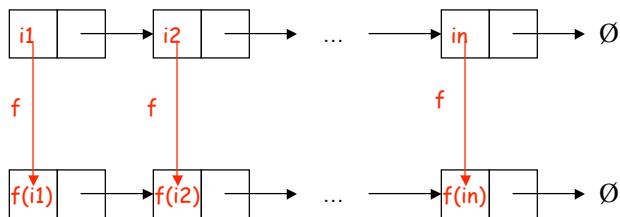
Review: mapSquares Illustrates the List Mapping Idiom



```
// Returns a new list whose elements are the squares
// of the corresponding elements in the given list
public static IntList mapSquares (IntList list) {
    if (isEmpty(list)) { // base case
        return empty(); // could use list instead
    } else { // recursive case
        return prepend(head(list) * head(list), mapSquares(tail(list)));
    }
}
```

More lists 15a-9

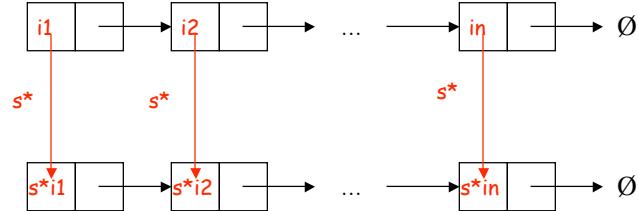
The General Mapping Idiom



```
public static IntList mapF (IntList list) {
    if (isEmpty(list)) { // base case
        return empty(); // could use list instead
    } else { // recursive case
        return prepend(f(head(list)), mapF(tail(list)));
    }
}
```

More lists 15a-10

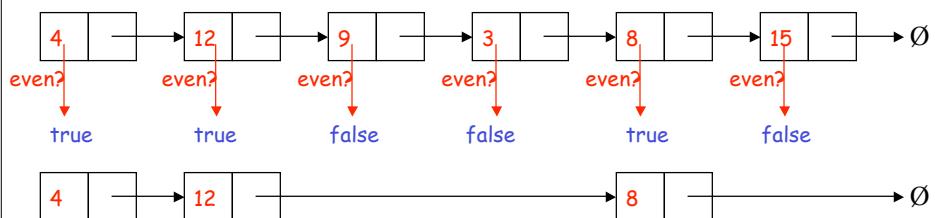
Mapping Sometimes Needs Extra Arguments



```
public static IntList mapScale (int s, IntList list) {
    if (isEmpty(list)) { // base case
        return empty(); // could use list instead
    } else { // recursive case
        return prepend(s * head(list)), mapScale (s, tail(list));
    }
}
```

More lists 15a-11

filterEvens Illustrates the List Filtering Idiom

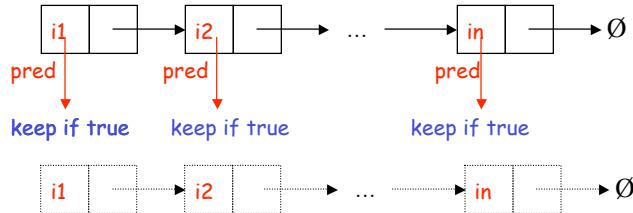


```
// Returns a new list whose elts are the even elts of the given list
public static IntList filterEvens (IntList list) {
```

}

More lists 15a-12

The General List Filtering Idiom



```
// Returns a new list whose elts satisfy predicate pred from given list
public static IntList filterPred (IntList list) {
    if (isEmpty(list)) {
        return empty();
    } else if (pred(head(list))) {
        return prepend(head(list), filterPred(tail(list)));
    } else {
        return filterPred(tail(list));
    }
}
```

More lists 15a-13

Filters sometimes need extra arguments

```
// Returns a new list whose elts are divisors of n from given list
public static IntList filterDivisors(int n, IntList list) {
    if (isEmpty(list)) {
        return empty();
    } else if ((n%(head(list))) == 0) {
        return prepend(head(list), filterDivisors(n, tail(list)));
    } else {
        return filterDivisors(n, tail(list));
    }
}
```

```
>IntListOps.filterDivisors(36, IntList.fromString("[2,3,4,5,6,7,8,9]"))
[2,3,4,6,9]
>IntListOps.filterDivisors(37, IntList.fromString("[2,3,4,5,6,7,8,9]"))
[]
```

More lists 15a-14

fromTo illustrates the List Generation Idiom

// Returns a list of the elements between from and to

```
public static IntList fromTo(int lo, int hi) {
```

```
}
```

➤ IntListOps.fromTo(3,7)

[3,4,5,6,7]

➤ IntListOps.fromTo(-4,12)

[-4,-3,-2,-1,0,1,2,3,4,5,6,7,8,9,10,11,12]

More lists 15a-15

Lists Enhance Modularity

Can implement many methods in terms of standard methods that produce and consume lists. For example:

```
public static int factorial (int n){  
    return prodList(fromTo(1,n));  
}
```

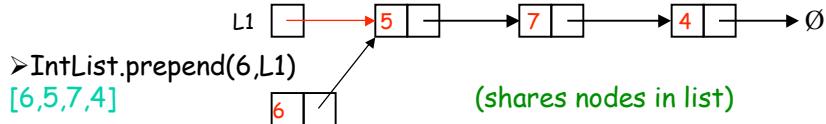
```
public static sumOfSquaredEvens (int lo, int hi){  
    return sumList(mapSquare(filterEven(fromTo(lo, hi))));  
}
```

Note that these methods are not recursive! The recursion is hidden in the standard list-processing methods.

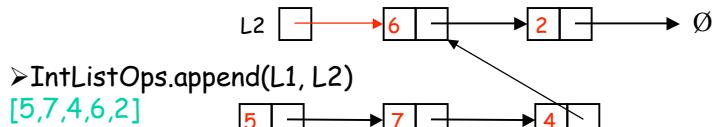
More lists 15a-16

List Glue

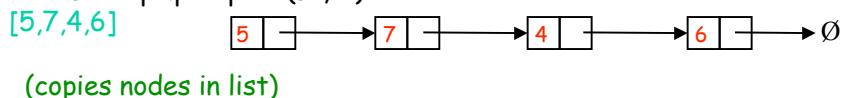
➤ `IntList L1 = IntList.fromString("[5,7,4]");`



➤ `IntList L2 = IntList.fromList("[6,2]");`



➤ `IntListOps.append(L1, L2)`



More lists 15a-17

append(IntList list1, IntList list2)

```
// Returns a list containing the elements of the first list
// followed by the elements of the second list. The nodes of the
// first list are copied, but the nodes of the second list are shared.
public static IntList append(IntList list1, IntList list2) {
```

```
}
```

More lists 15a-18

Invocation Tree for append(L1,L2)

More lists 15a-19

postpend(IntList list, int n)

```
// Returns a list containing the elements of the list followed by n.  
// The nodes of the list are copied, and a new node is made for n.  
public static IntList postpend (IntList list, int n) {
```

```
}
```

More lists 15a-20

reverse (IntList list)

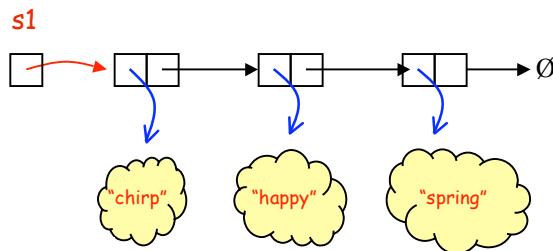
```
> IntListOps.reverse(IntList.fromString("[6,5,7,4]))  
[4,7,5,6]  
> IntListOps.reverse(IntList.fromString("[5,7,4]"))  
[4,7,5]  
> IntListOps.reverse(IntList.empty())  
[]  
// Returns a new list containing the elements of the given list  
// in reverse order.  
public static IntList reverse (IntList list) {  
    if (isEmpty(list)) {  
        } else {  
            }  
    }  
}
```

More lists 15a-21

Invocation Tree for reverse(L1)

More lists 15a-22

Lists are not just for ints



More lists 15a-23

Five core `StringList` methods

`public static String head (StringList L)`

Returns the string that is the head component of the list of strings node `L`.

`public static StringList tail (StringList L)`

Returns the list of strings that is the tail component of the list of strings node `L`.

`public static boolean isEmpty (StringList L)`

Returns `true` if `L` is an empty list of strings and `false` if `L` is a list of strings node.

`public static StringList empty()`

Returns an empty list of strings.

`public static StringList prepend (String x, StringList L)`

Returns a new list of strings node whose head is `x` and whose tail is `L`.

More lists 15a-24

Everything we did before, we can do now

```
// count the number of elements in a StringList
public static int length (StringList list) {
    if (isEmpty(list)) { // Really StringList.isEmpty
        return 0;
    } else {
        return 1 + length(tail(list)); // Really StringList.tail
    }
}
```

or

```
public static int length (StringList list) {
    return isEmpty(list)? 0 : 1 + length(tail(list));
}
```

More lists 15a-25

We can even make lists of lists!

- o Sometimes we need keep more than one list at a time.
Multiple lists might be organized as "lists of lists."
- o List of all subsets of the set [1,2,3]:
$$[[], [1], [2], [3], [1,2], [2,3], [1,3], [1,2,3]]$$
- o List of tails of the list [7, 1, 4]:
$$[[7, 1, 4], [1, 4], [4], []]$$

We'll say more about these in a later lecture.

More lists 15a-26