

Spirals, Trees, and Snowflakes

TurtleWorld

Tuesday, October 17, 2006

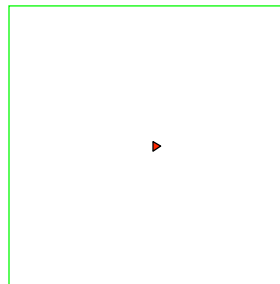


CS111 Computer Programming

Department of Computer Science
Wellesley College

Honey, I shrunk the Buggle

- o Turtles* are like Buggles, only smaller** and more carefree (no grid).
- o To create a new Turtle
`new Turtle();`
- o At birth, Turtles are centered, pointing EAST, pen*** down, and red.



* If you have programmed in LOGO, Turtles should be old friends.

** So small, in fact, that you cannot see them.

*** Turtles have pens rather than brushes.

TurtleWorld 11-2

Turtle Commands

Go Forward: `public void fd (double dist);`
Go Backward: `public void bd (double dist);`
Turn Left: `public void lt (double angle);`
Turn Right: `public void rt (double angle);`
Pen Up: `public void pu();`
Pen Down: `public void pd();`
Get Heading: `public double getHeading();`
Set Heading: `public void setHeading (double newHeading);`
Get Color: `public Color getColor();`
Set Color: `public void setColor (Color newColor);`
Get Position: `public double getX(); public double getY();`
Set Position: `public setX(double newX); public setY(double newY);`
`public setPosition(double newX, double newY);`
Go Home (to point (0,0), facing east, pen down): `public void home ();`

* When a `double` parameter is specified, Java will automatically convert an `int` argument to a `double`. E.g. `fd(36);` is treated like `fd(36.0);`

TurtleWorld 11-3

What's a double?

It's a `double`-precision floating point number. E.g.:

```
double x = 3.72;
x + 1.234 // Value = 4.954
x + 2 // Value = 5.72 (2 automatically converted to 2.0 first)
x * 2 // Value = 7.44 (2 automatically converted to 2.0 first)
x / 2 // Value = 1.86 (2 automatically converted to 2.0 first)

(int) x // Value = 3 ("int cast", converts to integer by truncation)
Math.round(x) // Value = 4 (rounds to nearest integer)
Math.floor(x) // Value = 3 (rounds toward negative infinity)
Math.floor(-5.12) // Value = -6 (rounds toward negative infinity)
Math.ceiling(x) // Value = 4 (rounds toward positive infinity)
Math.ceiling(-5.12) // Value = -5 (rounds toward positive infinity)

(double) 17 // Value = 17.0 ("double cast", converts to a double)
```

TurtleWorld 11-4

Be Careful with Division

`7/2 // Value = 3 (integer division)`

`7.0/2 // Value = 3.5 (floating point division)`

`7/2.0 // Value = 3.5 (floating point division)`

`7.0/2.0 // Value = 3.5 (floating point division)`

`((double) 7)/2 // Value = 3.5 (floating point division)`

`7/((double) 2) // Value = 3.5 (floating point division)`

`((double) 7)/((double) 2) // Value = 3.5 (floating point division)`

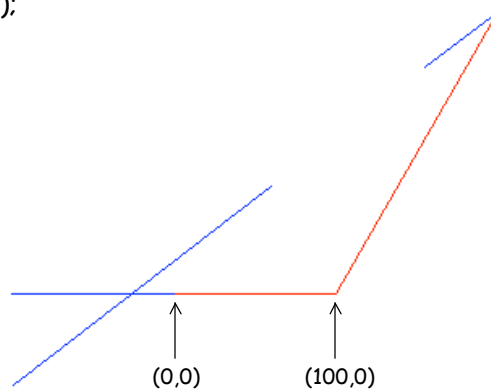
`(double) 7/2 // Value = ((double) 7)/2 = 3.5 (floating point division)`

`(double) (7/2) // Value = 3.0 (result of integer division
// converted to double)`

TurtleWorld 11-5

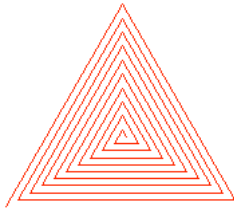
Myrtle the Turtle Goes on a Hike

```
public void run() {  
    Turtle myrtle = new Turtle();  
    myrtle.fd(100);  
    myrtle.lt(60);  
    myrtle.fd(200);  
    myrtle.rt(22.5);  
    myrtle.setColor(Color.blue);  
    myrtle.bd(56.78);  
    myrtle.pu();  
    myrtle.bd(120);  
    myrtle.pd();  
    myrtle.bd(200);  
    myrtle.home();  
    myrtle.bd(100);  
}
```

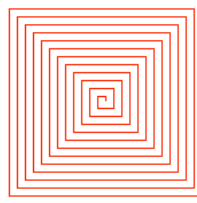


TurtleWorld 11-6

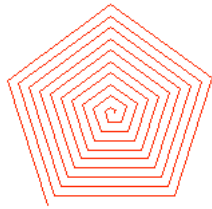
Spiro the Spiraling Turtle



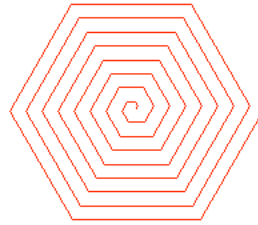
`spiro.spiral(30,120,0,6);`



`spiro.spiral(50,90,0,3);`



`spiro.spiral(50,72,0,2);`



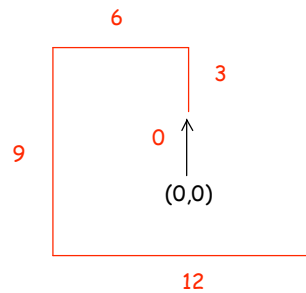
`spiro.spiral(40,60,0,6);`

TurtleWorld 11-7

`spiral(steps, angle, length, increment);`

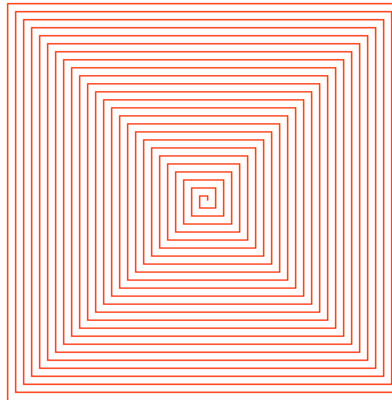
E.g., `spiral(100, 90, 0, 3);`

length
100 steps remain `fd(0);` angle
99 steps remain `lt(90);` increment
98 steps remain `fd(0+3);`
97 steps remain `lt(90);`
96 steps remain `fd(3+3);`
95 steps remain `lt(90);`



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After 100 Steps:



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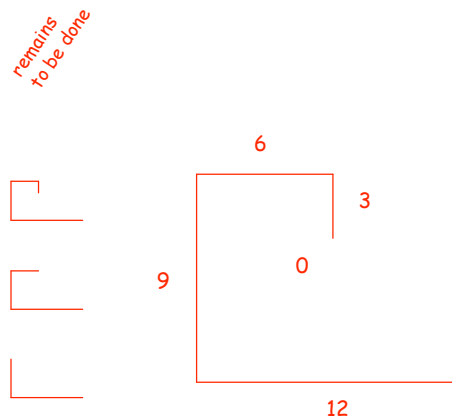
Designing a Java spiral() Method

Think invocation trees!

```

      steps  angle  length  increment  remains
      to be done
spiral(5, 90, 0, 3);
  fd(0);
  lt(90);
  spiral(4, 90, 3, 3);
    fd(3);
    lt(90);
    spiral(3, 90, 6, 3);
      fd(6);
      lt(90);
      spiral(2, 90, 9, 3);
        fd(9);
        lt(90);
        spiral(1, 90, 12, 3);
          fd(12);
          lt(90);
          spiral(0, 90, 12, 3);

```



TurtleWorld 11-10

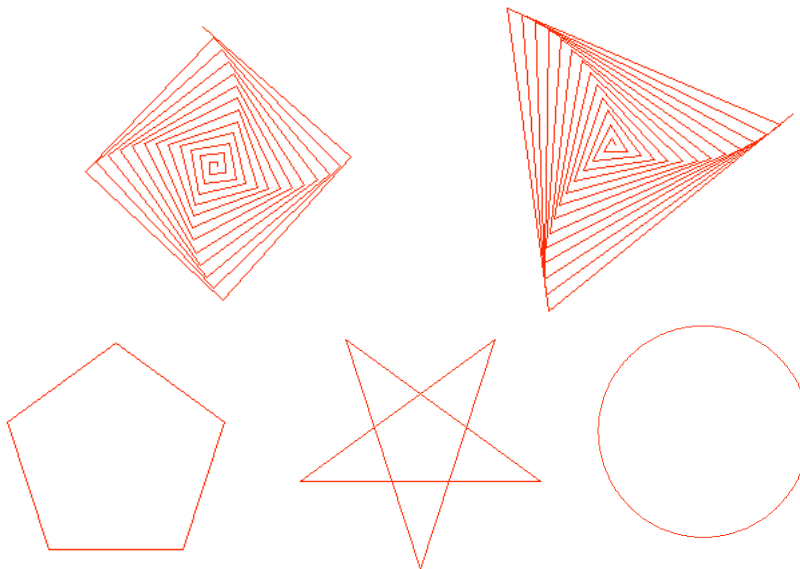
Let's Write the spiral() Method in Java

```
public void spiral(int steps, double angle,
                  double length, double increment)
{
```

}

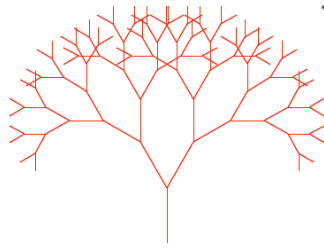
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How Do You Draw These with spiral()?

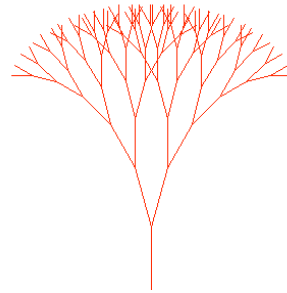


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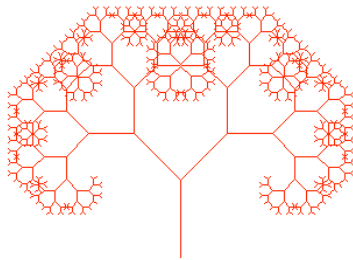
TreeWorld



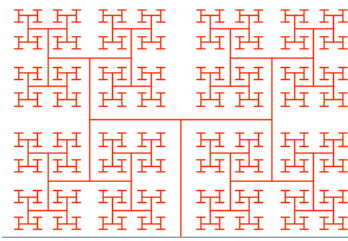
`trina.tree(7,75,30,0.8)`



`trina.tree(7,75,15,0.8)`



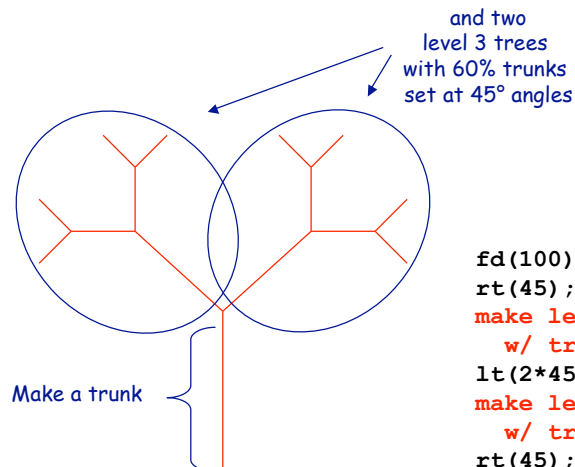
`trina.tree(10,80,45,0.7)`



`trina.tree(10,100,90,0.68)`

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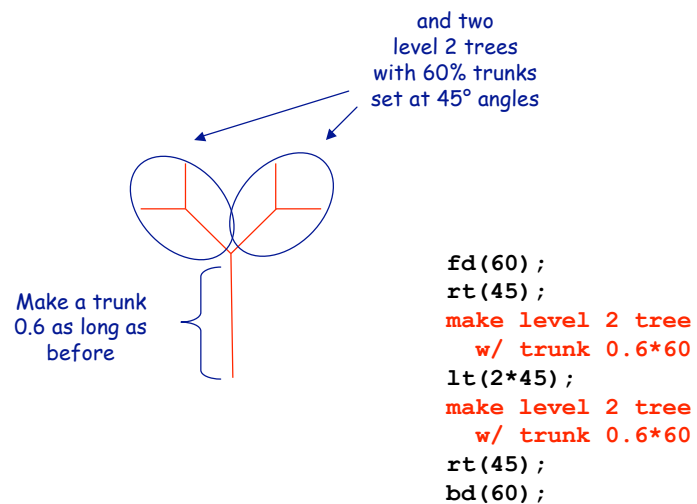
How to make a level 4 tree



```
fd(100);
rt(45);
make level 3 tree
w/ trunk 0.6*100
lt(2*45);
make level 3 tree
w/ trunk 0.6*100
rt(45);
bd(100);
```

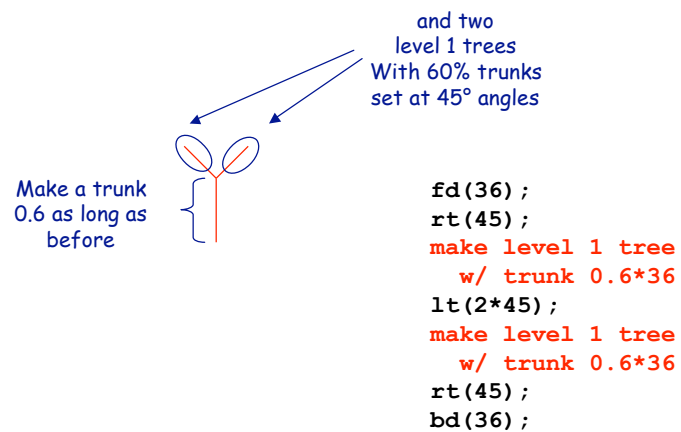
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How to make a level 3 tree



TurtleWorld 11-15

How to make a level 2 tree



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How to make a level 1 tree

Make a trunk
0.6 as long as
before



and two
level 0 trees
set at 45° angles

```
fd(21.6) ;  
rt(45) ;  
make level 0 tree  
  w/ trunk 0.6*21.6  
lt(2*45) ;  
make level 0 tree  
  w/ trunk 0.6*21.6  
rt(45) ;  
bd(21.6) ;
```

TurtleWorld 11-17

How to make a level 0 tree

Do nothing!

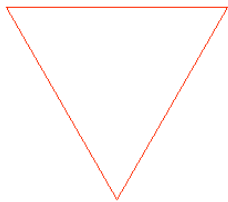
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Let's Write tree() in Java

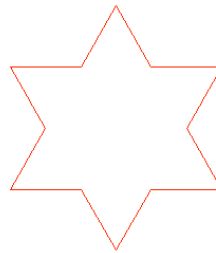
```
public void tree(int levels, double length,
                 double angle, double shrink) {
```

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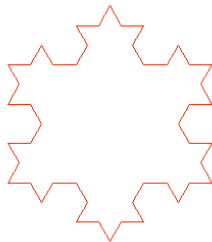
Snowflakes (the Koch curve)



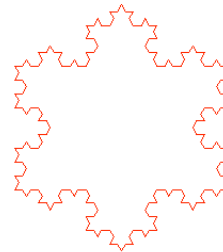
```
snowy.snowflake(0.200);
```



```
snowy.snowflake(1.200);
```



```
snowy.snowflake(2.200);
```



```
snowy.snowflake(3.200);
```

TurtleWorld 11-20

A Snowflake has 3 Sides

```
public void snowflake (int levels, double length) {
    snowside(levels, length);
    rt(120);
    snowside(levels, length);
    rt(120);
    snowside(levels, length);
    rt(120);
}
```

```
snowy.snowside(0,200);
```

```
snowy.snowside(1,200);
```

```
snowy.snowside(2,200)
```

```
snowy.snowside(3,200);
```

TurtleWorld 11-21

Let's Write snowside() in Java

```
public void snowside (int levels, double length) {
```

TurtleWorld 11-22